CROP ECOLOGY, MANAGEMENT & QUALITY

Root-Zone Salinity: I. Selecting a Product–Yield Index and Response Function for Crop Tolerance

H. Steppuhn,* M. Th. van Genuchten, and C. M. Grieve

ABSTRACT

Six empirical functions were compared for describing the product yields of agricultural crops grown while subject to increasing levels of root-zone salinity. The four nonlinear functions fit the test data from a spring wheat (Triticum aestivum L., cv. Biggar) experiment conducted in Canada’s Salt Tolerance Testing Facility closer than the two linear functions. Although each of the four nonlinear declining functions could reasonably describe the data, the modified compound-discount equation recorded the lowest root mean square error and the highest R² value. Additional response data using the nonlinear discount function obtained from 33 separate trials averaged 11% closer in statistical fit and 45% lower in statistical error than the best linear function. The discount function \( Y = \frac{1}{1 + \frac{(C/C_0)\cdot e^{-r t}}{1.06}} \) follows a sigmoidal form and relates relative yield \( (Y_t) \) to a measure of root-zone salinity \( (C) \) such as the solute concentration with an electrical conductivity of an equivalent saturated soil paste extract (EC). This function features two parameters, the salinity level producing 50% of the nonsaline crop yield \( (C_{50}) \) and the absolute value of the general decline in relative yield with salinity at and near \( C_{50} \), the steepness constant \( (s) \). These parameters combine to form a single-value, salinity-tolerance index (ST-Index) consisting of the 50% reduction in crop yield \( (C_{50}) \) plus the tendency to maintain some product yield as the crop is subjected to increasing salinity levels approaching \( C_{50} \), i.e., ST-Index = \( C_{50} + s(C_{50}) \). The ST-Index for the Biggar wheat registered 6.44. Approximations for \( C_{50} \) and \( s \) can be derived from the threshold salinity \( (C) \) and declining slope \( (b) \) parameters of the threshold-slope linear response function \( Y = 1 - b(C - C_0) \). Procedures for converting \( C \) to \( C_{50} \) and \( b \) to \( s \) offer linkages between these linear and nonlinear response function parameters, and are further explored in this paper’s companion. The resulting ST-Index-values equal 6.56, 9.43, and 5.67 for sample field (corn, Zea mays L.), forage (alfalfa, Medicago sativa L. and falcata L.), and vegetable (radish, Raphanus sativus L.) crops, respectively.

LABORATORY AND FIELD TESTS to identify decreases in crop yield in response to increasing root-zone salinity have been conducted for many years and are listed by Francois and Maas (1978, 1985) and Ulery et al. (1998), among others. The inherent ability of crop plants to withstand the effects of elevated solute concentrations in their root-zone solutions and still produce a measurable agricultural product defines the magnitude of crop tolerance or resistance to salinity. Salinity generally slows the rate of crop growth, resulting in plants with smaller leaves, shorter stature, and reduced economic yield (Shannon et al., 1994). The degree to which growth is curtailed by salinity differs with crop species and variety (Shannon and Grieve, 1999).

In this study, we briefly review the factors that affect the response of crops to root-zone salinity, summarize and evaluate a number of models that have or could be used for the crop salt tolerance response function, and propose a Salinity Tolerance Index that provides a relative ranking of crops according to their tolerance to root-zone salinity.

CROP YIELD RESPONSE TO SALINITY

Ayers and Westcot (1985) define a salinity problem as a condition where the salts in solution within the crop root zone accumulate in concentrations which decrease crop yield. Although all dissolved solids and gasses contribute ions to the total concentration, these authors, writing for FAO, list the most common excess constituents as calcium, magnesium, sodium, carbonate, bicarbonate, chloride, sulfate, nitrate, ammonium, phosphate, potassium, boron, and various trace elements. Solutes in aqueous solutions decrease osmotic potential, which affects plant water uptake (Wadleigh and Ayers, 1945; Munns and Termaat, 1986; Jacoby, 1999; Katerji et al., 1997). Osmotic effects contribute to reduced growth rate, changes in leaf color, and developmental characteristics, such as root/shoot ratio and maturity rate. In addition, ion toxicities or nutritional deficiencies may arise as a result of the excessive presence of specific ions and/or a competition among specific cations or anions (Bernstein, 1974; Torres-Bernal et al., 1974; Shannon and Grieve, 1999). Ionic effects are often manifested by leaf and meristem damage or as symptoms typical of nutritional disorders. For example, Na or Cl ions may accumulate in plant leaf tissue and cause necrotic tips and/or margins (Bernstein et al., 1956; 1969). Salinity-induced nutritional deficiencies present symptoms generally similar to those that occur in the absence of salinity. Often cited is the presence of sulfate and large Na/Cl ratios in root-zone solutions which were thought to lead to symptoms of calcium deficiency (Maas and Hoffman, 1977; Janzen and Chang, 1987, 1988). More commonly,

Abbreviations: ECs, electrical conductivity of saturated soil paste extract; ECi, electrical conductivity of the irrigated water; ECt, electrical conductivity of test solution; FAO, Food and Agriculture Organization, United Nations; ST-Index, salinity tolerance index.
nutritional effects tend to work in conjunction with specific ion toxicity but vary in their degree of manifestation in different crops (Curtin et al., 1993; Grattan and Grieve, 1999).

Salinity is commonly measured in units of electrical conductivity at 25°C and an electrode spacing of 10 mm. Representative soil samples are obtained from the root zone to which deionized water is added to derive saturated-paste extracts following standard procedures (Rhoades, 1982). The electrical conductivity (ECe) of these extracts provides a consistent, repeatable, and widely accepted salinity standard (U.S. Salinity Laboratory Staff, 1954). An advantage of using ECe as a salinity measure is that it relates to saturated field soil water conditions. Other measures of root-zone salinity include solute concentration (C) and osmotic potential (Ψs) of the soil extracts. For many soil extracts,

\[ \text{ECe} = 640 \ (C) \]  

and \[ \Psi_s = -36.47 \ (\text{ECe}) \]  

where ECe, C, and Ψs are respectively expressed in decisiemens per meter (dS/m), parts per million (ppm), and kilopascals (kPa) (U.S. Salinity Laboratory Staff, 1954). Experience has also shown that the electrolyte concentration resulting from the saturated soil-paste-extract procedure equals approximately one-half that of the soil pore water at field capacity (Ayers and Westcot, 1985).

The relative effects of specific ions in root-zone solutions compared with decreased osmotic potential resulting from elevated solute concentrations has been debated at length. Palmer (1937) noted that adding Na2SO4 to potted soils was more injurious to cereals than adding soil may act as either an ion source or sink. Variations in the yields of garden beets, wax beans, or carrots cause considerable variations in the resulting crop yields. Maas (1990) cited the work of Bernstein in suggesting that upward salt-tolerance adjustments of 1 to 3 dS/m are appropriate where calcium sulfate salinity dominates soil solutions to apply crop yield data obtained at the same ECe in chloride-dominated response tests.

Crops have been tested for salt tolerance in both field and greenhouse experiments in soil and sand cultures. Yaron et al. (1972) studied regression procedures for estimating the yield of field-grown crops in response to soil water content and salinity. Using grapefruit (Citrus × paradisi Macf.) and peanut (Arachis hypogaea L.) data, they identified many of the difficulties associated with correlating yield with salinity when soil water contents vary. Typically, randomly arrayed field plots or large tanks containing the crops under investigation are separately salinized artificially with an irrigated solution whose solute concentration equates to one of a range of increasing salinities. In the field, within soil, the time required for complete mixing and diffusion of the irrigated test solutions with the initial soil solutions through-and-through the root zone can require days or weeks or longer as compared to minutes or hours for greenhouse sand cultures. Field tests with soil provide greater opportunity for evapotranspiration or rainfall to concentrate or dilute the in situ, dissolved salts, especially following infrequent applications of saline test solutions. Unless growing conditions carefully duplicate those of the target growing season, greenhouse testing can also cause skewed responses. In addition, field-based, salt-tolerance testing may have to contend with preferential flow and with spatial and temporal salinity transients in the root zones. Unless irrigated with large leaching fractions, the soil may act as either an ion source or sink. Variations in the actual solute concentration of the solutions acting on the roots of test crops, especially in field trials, can cause considerable variations in the resulting crop yields.

Besides changes in solute concentrations, many other crop–environment interactions may cause variations in salinity–yield relationships, such as those involving temperature, radiation, humidity, atmospheric pollutants, wind, soil water content, and fertility (Shannon et al., 1994). The combination of high temperatures and low humidity may decrease crop salt tolerance, especially if soil water reserves are limited (Bernstein, 1974). Hoffman et al. (1978) observed that pinto bean grown in a cool, humid environment tolerated higher salt levels than those predicted from published data. Drought often combines with salinity adding to the difficulties faced by crop plants (Bresler et al., 1982; Katerji et al., 1992; Feng et al., 2003a, 2003b). Testing for crop salt tolerance involves separating the simultaneous effects of any water deficits from those resulting from the salinity. Root-zone fertility and aeration in the absence or presence of salinity contribute eminently to the productivity of crop plants. Doughty and Stalwick (1940), Lunin et al. (1961a, 1963), Ravikovich and Porath (1967), Ravikovich and Yoles (1971), Bernstein (1974), and Peters (1983) are among many who reported salinity–fertility interactions affecting interpretations of salt-tolerance data. If the yield response to increasing root-zone salinity encounters nutrient or oxygen deficits, a threshold...
limit for maximum productivity typically results (Maas and Hoffman, 1977). Shallow water tables or very frequent irrigation can cause poor soil aeration, and thereby, negatively affect the testing of crops for their tolerance of salinity, as exemplified in tomato and wheat (Aubertin et al., 1968; Aceves-N et al., 1975).

Plant ontogeny or growth stage also affects crop tolerance of salinity. For example, turnip (Brassica rapa L.) is most salt tolerant at germination, but more sensitive as a seedling than at harvest (Francois, 1984). In general, the earlier and longer that crop plants must cope with root-zone salinity, the greater the reduction in vegetative growth (Lunin et al., 1961b, 1962, 1963; Kaddah and Ghowail, 1964; Francois et al., 1994; Katerji et al., 1998). A common practice in testing crop plants for their salinity tolerance is to delay salinization of root zones until after the plants have been established (Maas and Grattan, 1999). Delaying salinization from sowing to establishment causes variation in crop yields (Lunin et al., 1962; Steppuhn et al., 1996). In wheat, delaying salinization beyond emergence increases the number of primordia, the final leaf number, and likely the grain weight (Grieve et al., 2001a). Even the same variety can respond differently depending on the interactions of phenology and the initiation of the root-zone salinity (Shannon and Noble, 1990).

Genetic, physiological, and ecological crop differences combine to determine how a crop will respond to salinity. Wheat, for example, varies in tolerance among many of its varieties, cultivars, and strains (Torres-Bernal and Bingham, 1973; van Hoorn et al., 1993; Steppuhn and Wall, 1997). At the same time, plants grown from larger seeds, at least for two wheat cultivars, tend to show better salinity tolerance than plants from smaller seeds (Grieve and Francois, 1992). Ecologically, crop yields in saline environments vary in their response to plant density. In wheat, widely spaced crop plants tend to show the effects of saline root-zones more than closer spaced plants (L.E. Francois, personal communication; Steppuhn, 1997). The distinction between testing for salt tolerance among agricultural crops rather than among agricultural plants guides the discussion and work presented herein.

Most lists of the relative salinity tolerance among agricultural crops are based on comparisons of parameters in specific salinity–yield functional relationships (van den Berg, 1950; U.S. Salinity Laboratory Staff, 1954; Allison, 1964; Bernstein, 1974; Maas and Hoffman, 1977; Bresler et al., 1982; Maas, 1986; Francois and Maas, 1994; Maas and Grattan, 1999). The parameters in these functions have come to serve as indices for salinity tolerance. The objective of this study was to compare various yield functions to suggest a general response and index, which, though empirical, most closely reflects the general response of agricultural crops to root-zone salinity.

**RESPONSE FUNCTIONS**

Crops produce a wide array of agricultural commodities and do so with efficiencies measured by crop yield. Yields vary depending on crop species, cultivar, ambient environment, soil fertility, pest damage, and many other factors besides salinity. Yields also vary because the commodities produced from plant crops originate from a diverse array of plant components: leaves, stems, flowers, fruits, seeds, roots, tubers, and other tissues. To compare the tolerance of crops to root-zone salinity, yields are usually standardized and expressed on a relative basis. The usual procedure for converting absolute yield (Y) to relative yield (Y_r) employs a scaling divisor (Y_m) based on the production where salinity has very little or no influence on yield (Maas, 1990). Such a divisor normalizes the data set, and almost always equals the maximum yield resulting from the response test. A Y_r value is determined for each cultivar in each test by

\[ Y_r = \frac{Y}{Y_m} \]  

Various empirical equations have been applied or suggested for describing Y_r as a function of a variable, which reflects the average root-zone salinity (C). Measures used for C have included C_s, Ψ_w, EC_e, and EC_i, where EC equals the electrical conductivity of the irrigation water.

**Simple Linear Function**

Early analyses of crop yield responses to salinity commonly followed a simple linear relationship of the form

\[ Y_r = a - b(C) \]  

Researchers restrictively applied a fitted linear function over the range of the salinities tested, or they simply showed the plotted response points without a fitted function (Palmer, 1937; Magistad et al., 1943; Ayers et al., 1943; Wadleigh and Ayers, 1945; Batchelder et al., 1963; Holm, 1983). Rarely, if ever, were the regression coefficients a and b identified as representing any biophysical characteristics of the response.

**Modified Weibull Function**

The statistical Weibull cumulative probability distribution exponentially relates one variable to another and increases in value from zero to one as the independent variable ranges from its upper to its lower values (Weibull, 1951). Used as a response function to root-zone salinity, the Weibull distribution has been modified and expressed in terms of the proportionate Y_r yield remaining at any C as follows:

\[ Y_r = \exp[a(C^b)] \]  

where the regression coefficient a is always negative and defines the intensity of the relationship, and the constant b reflects the shape of the response curve. Neither a nor b specify any distinct biophysical characteristic. The modified Weibull function has served as an analog for the response of crop growth or yield to environmental toxicity and solute excess (Rawlings and Cure, 1985; Taylor et al., 1991; Jalil et al., 1994a, 1994b).

**Bi-Exponential Function**

van Genuchten (1983) included a more general exponential response function for analyzing crop salt-tolerance data,
the empirical constants \(a\) and \(b\) again lack any biophysical identity and can be evaluated by nonlinear regression. van Genuchten and Hoffman (1984), Steppuhn et al. (1996), and Wang et al. (2002) used the bi-exponential function to describe the yield-responses of perennial ryegrass (Lolium perenne L.), wheat, and elephant grass (Pennisetum purpureum Schum.), respectively.

**Modified Gompertz Function**

According to Lapp and Skoropad (1976) actuaries for many years used a form of an equation proposed by Gompertz (1825) to predict human mortality. In various forms, the same equation has been applied in botany to model germination (Tipton, 1984), emergence (Gan et al., 1992), and growth (Baker et al., 1975). Steppuhn et al. (1998) compared the emergence of two Russian wild ryegrass cultivars from saline seedbeds with the Gompertz function. In the following form, it can also serve as a crop-yield salinity response function:

\[
Y_t = 1 - \exp[a \exp(bC)]
\]  

where empirical constants \(a\) and \(b\) are always negative, lack any biophysical identity, and can be evaluated by nonlinear regression.

**Three-Piece Linear (Threshold-Slope) Function**

After reviewing the yield responses measured in a large number of root-zone salinity experiments conducted worldwide, Maas and Hoffman (1977) introduced a two-piece linear model for the response of agricultural crops to increasing salinity. This resulted in their now classic threshold-slope concept. In its most general form, this model can be written as a three-piece response function (van Genuchten, 1983):

\[
Y_t = \begin{cases} 
1 & 0 < C < C_1 \\
1 - b(C - C_i) & C_1 < C < C_0 \\
0 & C > C_0 
\end{cases}
\]  

where \(b\) is the absolute value of the declining slope in \(Y_t\) with \(C\); \(C_i\) is the maximum value of salinity without a yield reduction (the threshold \(C\)); \(C_0\) is the lowest value of \(C\), where \(Y_t = 0\). The empirical constants, \(b\) and \(C_i\), are usually evaluated by regression and/or visual inspection. Maas and Hoffman (1977) introduced their model as a two-piece expedient, ignoring the third segment, the yield response beyond \(C_0\). They also defined the “threshold salinity” \(C_i\) and the “slope” \(b\), as characteristics that are uniquely specific to each crop, but gave no biophysical reasons for the existence of these characteristics. Maas and Hoffman (1977) also manually fitted the threshold-slope function to data for some 60 crops using experimental salt-tolerance field data reported in the literature. They included reports from experiments in which crops were grown while subjected to two or more levels of salinity plus a nonsaline control. For 25 yr, their threshold-slope values have served as first approximations of crop salinity tolerance. The value of their work is that it demonstrated the use of mathematical response functions and associated parameters to evaluate and compare the salinity tolerance of crops. Feinerman and Yaron (1982) extended the threshold-slope response function to include the effects of soil moisture with all other factors assumed constant.

**Modified Discount Function**

The compound discount equation can be modified into a sigmoidal-shaped response function,

\[
Y_t = 1/(1 + (C/C_s)^{exp(C_o)})
\]  

where \(C_s\) defines \(C\) at \(Y_t = 0.5\), and \(s\) represents the response curve steepness. The steepness parameter equals the average absolute value of the slope \((dY/dC)\) of the equation through \(C_s\) and its steepest segments on either side of \(C_s\), evaluated in our study from \(Y_t = 0\). The argument \(sC_s\) of the exponent in Eq. [9] contributes to a symmetrical concave-convex yield response with the inflection point at \(C_s\) and is analogous to the product \(bC\) of the threshold-slope model (Eq. [8]). Both \(s\) and \(b\) indicate unit decreases in relative product yield with unit increases in root-zone salinity. As in the threshold-slope function, the modified discount function features parameters \((s\) and \(C_s\)\) with identifiable biophysical characteristics.

van Genuchten (1983) was the first to apply a form of the modified discount function to yield data of agricultural crops growing subjected to increasing root-zone salinity; he used the empirical constant \(p\) as the exponent instead of \(exp(sC_s)\):

\[
Y_t = 1/(1 + (C/C_s)^p)
\]  

In this form of the discount equation, \(p\) is a shape parameter without biophysical identity, which has been evaluated from 1 through 9 (van Genuchten and Gupta, 1993). In all reported applications of this form of the function, the value of \(p\) has always exceeded 1.0 (van Genuchten and Hoffman, 1984; van Genuchten and Gupta, 1993; Steppuhn, 1993; Steppuhn et al., 1996). This is related to the property of Eq. [10] that its slope at zero salinity \((C = 0)\) is zero for \(p\) values greater than 1, finite \((-1/C_s)\) when \(p = 1\), and \(-\infty\) when \(p < 1\), the latter case being unrealistic from a practical view.

**SALINITY TOLERANCE INDEX**

Before 1977, the concept of using an index to rate the salinity tolerance of agricultural crops was consistently followed (Ayers et al., 1951; U.S. Salinity Laboratory Staff, 1954; Brown and Hayward, 1956). The practice was to simply use \(C_s\), derived directly from experimental data, as the index. The introduction of the threshold-slope function to assess the yield response of agricultural crops to increasing levels of root-zone salinity provided two functional parameters \((b\) and \(C_i)\) with which to index relative salt tolerance (Maas and Hoffman, 1977). These parameters served as dual indices resulting in various lists of the relative salinity tolerance among agricultural crops (Maas and Hoffman, 1977; Bresler et
As briefly reviewed in this study, many factors influence the yield of agricultural crops besides the response to increasing root-zone salinity. With a myriad of influences acting on the yield relationship, a single-value index of crop tolerance to root-zone salinity would seem sufficient for comparing the salinity tolerance of agricultural crops. If $C_{50}$ were enhanced by a term, which dictates the shape of the yield response for salinity levels approaching $C_{50}$, such as the argument of the exponent in Eq. [9], a comprehensive, single-value, Salinity Tolerance Index or ST-Index results:

\[
\text{ST-Index} = C_{50} (1 + s) \quad [11]
\]

where $C_{50}$ and $s$ can be computed as regression constants, or approximated by a visual inspection of the response data. The shape of the function for salinity levels greater than $C_{50}$ is not included in this index.

### MATERIALS AND METHODS

The crop-yield response data selected for comparing the functional effects to root-zone salinity on crops were obtained from Canada’s Salt Tolerance Testing Laboratory (Steppuhn and Wall, 1999). A spring-seeded wheat cultivar, Biggar, was tested for salinity tolerance in an environmentally controlled greenhouse (Steppuhn and Wall, 1997). Biggar produces flour with medium protein, medium gluten, and medium kernel hardness for world trade (DePauw et al., 1991).

The Biggar wheat crop was grown in plastic tanks (0.85-m diam., 1.0 m deep cylinders) containing washed silica sand (99.8% pure) having an average bulk density of 1.5 Mg m$^{-3}$. At saturation, the sand has a mean volumetric water content of 31.3%. In this test, the tanks were flushed four times daily with a modified Hoagland nutrient solution consisting of 2.0 mM Ca(NO$_3$)$_2$, 2.5 mM KNO$_3$, 0.17 mM KH$_2$PO$_4$, 1.0 mM MgSO$_4$, 0.05 mM chelated Fe, 0.5 mM NH$_4$NO$_3$, 0.05 mM KCl, 0.023 mM H$_2$BO$_3$, plus trace elements including Mn, Zn, Cu, Si, and Mo. Solutions were salinized by adding NaCl and CaCl$_2$ (1:1 by mass) resulting in pH values of 7.5 to 7.9. Each irrigation continued for five minutes until the sand was completely saturated after which the solutions drained into 612-L reservoirs for the next irrigation. Water lost by evapotranspiration was replenished weekly or more frequently when the volume of the solution in the supply reservoir decreased by 3% or more. The electrical conductivity of each solution was checked initially, weekly, and at harvest.

Eleven treatment solutions were prepared with solution electrical conductivities targeted at 2, 3, 4, 6, 8, 10, 12, 16, 20, 24, and 28 dS m$^{-1}$. The relative variability in grain yield which likely would occur in association with each conductivity was estimated from previous experiments. These estimates divided by an error tolerance squared and multiplied by an appropriate $t$-table value squared indicated the treatment replication necessary to maintain accuracy of the planned statistical regressions. The tank arrangement followed a randomized block design with respect to cultivars, but was modified slightly to eliminate any bias caused by taller plants blocking solar radiation associated with low sun angles. Forty-five Biggar wheat seeds were sown per tank on 3 Feb. 1993, 40 mm deep into the sand separated by 80 mm within rows spaced 150 mm apart. After emergence, populations were thinned to 35 plants per tank.

The procedure for adding salts to the irrigated solutions in this test approximated that practiced by the U.S. Salinity Laboratory (L.E. Francois, E.Y. Maas, and C.M. Grieve, personal communications). Salts were added gradually, with the first third on Day 13 after seeding (plants emerging), the second third on Day 18 (plants showing two leaves), and the final third on Day 22 (three leaves showing). Daylengths were adjusted during the growing period with 475 W sodium lamps positioned 1.5 m above the sand surfaces to mimic a typical field seeding date of 1 May at latitude 50°N. Mean temperatures equaled 24°C daytime and 18°C nighttime. The maximum daily ambient air temperature ranged from 22 to 26°C and the minimum between 16 and 19°C.

The response of the wheat crop to the salinity treatments at harvest was determined by weighing the oven-dried grain yield. Yield measurements were averaged and related to $E_C$ derived from the electrical conductivities of the test solutions ($E_C$) by the conventional relationship followed by the U.S. Salinity Laboratory (Maas, 1990),

\[
E_C = 0.5 E_{50} \quad [12]
\]

This equation assumes that the solutions fill the soil pores to field capacity and has been substantiated by Janzen and Chang (1988) and Kohut and Dudas (1994).

The optimal value of $Y_m$ is determined by substituting $Y/Y_m$ (Eq. [3]) for $Y_r$ for each of the response functions tested and estimating $Y_m$ by linear or nonlinear least-squares regression with the data set (van Genuchten, 1983). To ensure a common initial basis for comparing the six response functions with the Biggar wheat data, $Y_m$ was set equal to the yield of the first data pair, 307.0 g m$^{-2}$, obtained in the absence of root-zone salinity. With $Y_m$ determined, and $Y_r (Y/Y_m)$ computed, the different response functions were fitted to the $E_C$–data to test each model obtaining the associated root mean square error, coefficient of determination, and parameter estimates. Least-square fits were performed by the maximum neighborhood method of Marquardt (1963), which is based on an optimum interpolation between the Taylor series method and the method of steepest descent (Bates and Watts, 1988; SAS, 1995).

In addition to the Biggar wheat data, the absolute or relative yields found within 33 other studies from crops grown in increasingly saline rooting media were assessed. $R^2$ values and root mean square errors (RMS errors) associated with applications of the threshold-slope and modified discount equations to these additional data sets were computed and compared.

### RESULTS AND DISCUSSION

The decline in crop yield for Biggar wheat in response to increasing root-zone salinity corresponds similarly to the declines reported for spring-sown wheats in field salinity trials conducted by Holm (1983) and McKenzie (1988) during comparable daylengths and temperatures. Grain yields produced from the wheat grown under low salinity levels at first deviated only slightly from the nonsaline production (Table 1). As salinity increased, its incremental effect on yield increased to a maximum about midway or two-thirds into the response relationship. Thereafter, increasing salinity had a decreasingly reduced influence on yield. Any one of the functional plots resulting from the six test equations applied to the Biggar wheat test data could serve as an empirical analog of the relationship (Fig. 1–6). The three-piece linear function was determined by selecting the first three data pairs as points within the upper horizontal segment of
Table 1. Average absolute (Y) and relative (Yr) spring wheat grain yields (cv. Biggar) in response to irrigation with salinized solutions.

<table>
<thead>
<tr>
<th>Target ECi†</th>
<th>Actual ECi</th>
<th>ECe†</th>
<th>Y</th>
<th>Yr</th>
</tr>
</thead>
<tbody>
<tr>
<td>dS m⁻¹</td>
<td>g m⁻²</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2‡</td>
<td>1.96</td>
<td>0.98</td>
<td>307.0</td>
<td>1.0</td>
</tr>
<tr>
<td>3</td>
<td>3.11</td>
<td>1.55</td>
<td>306.9</td>
<td>0.999</td>
</tr>
<tr>
<td>4</td>
<td>4.20</td>
<td>2.10</td>
<td>282.9</td>
<td>0.921</td>
</tr>
<tr>
<td>6</td>
<td>6.24</td>
<td>3.12</td>
<td>234.9</td>
<td>0.765</td>
</tr>
<tr>
<td>8</td>
<td>8.12</td>
<td>4.06</td>
<td>225.4</td>
<td>0.734</td>
</tr>
<tr>
<td>10</td>
<td>10.60</td>
<td>5.30</td>
<td>170.0</td>
<td>0.554</td>
</tr>
<tr>
<td>12</td>
<td>12.08</td>
<td>6.04</td>
<td>111.0</td>
<td>0.362</td>
</tr>
<tr>
<td>16</td>
<td>16.34</td>
<td>8.17</td>
<td>82.6</td>
<td>0.269</td>
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<td>20</td>
<td>19.94</td>
<td>9.97</td>
<td>64.5</td>
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</tr>
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<td>24</td>
<td>24.20</td>
<td>12.10</td>
<td>19.9</td>
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</tr>
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<td>28</td>
<td>27.60</td>
<td>13.80</td>
<td>15.0</td>
<td>0.049</td>
</tr>
</tbody>
</table>

†ECi, electrical conductivity of the average irrigated test solution; ECe, approximate equivalent electrical conductivity of saturated soil-paste extract.
‡Nutrients (1 dS m⁻¹ plus background salinity of the hydroponic test water (1 dS m⁻¹)), considered nonsaline.

Fig. 1. Simple linear response function, \( Y_r = a - b(C) \), applied to the Biggar spring wheat data.

Fig. 2. Modified Weibull response function, \( Y_r = \exp[a(C)^b] \), applied to the Biggar spring wheat data.

Fig. 3. Bi-exponential response function, \( Y_r = \exp[aC - b(C^2)] \), applied to the Biggar spring wheat data.

The function. Other data-pair selections would have given different results.

The \( R^2 \) values from regression analyses using the six functions ranked from a low of 0.941 for the simple linear to a high of 0.988 for the modified discount relationship (Table 2). RMS errors ranged from a low of 0.0433 for the discount equation to a high of 0.0940 for the simple linear relationship. On the basis of the statistics in Table 2, the modified discount function is slightly better than the other nonlinear functions and considerably better than the linear models. In addition, the discount-based function features empirically derived parameters which represent the biophysical characteristics of mid-yield salinity \( (C_{0}) \) and generalize unit decline in yield with salinity \( (s) \). These discount parameters respectively dictate the position of the functional curve and the general steepness of the decline along the increasing scale of root-zone salinity. Only the threshold-slope model also features constants which identify biophysical parameters, threshold salinity \( (C_t) \), and linear decline in yield with salinity \( (b) \).

Additional \( R^2 \) and RMS error values, calculated for 33 other data sets (17 different crops) further demonstrate the greater utility of the modified discount function compared to the threshold-slope function (Table 3). Thirty-two out of 33 \( R^2 \) values and 30 out of 33 RMS errors favor the discount equation. Arithmetic averages from the 33 comparisons for the threshold-slope linear model \( R^2 \) and RMS error equal 0.815 and 0.1276, respectively. For the discount nonlinear model, the averages equal 0.904 and 0.0705, respectively. The modified-discount response function represents an improvement to the linear relationship, decreasing the average error by 45% and increasing the model-fit by an 11% average.

The literature offers no theoretical rationale for the existence of a \( C_t \). Taylor et al. (1991) even argue against it, stating, “There is no a priori reason to expect the relationship between yield and exposure to a metal ion to be discontinuous.” It is true that plant species have evolved various salt-tolerance mechanisms to cope with saline root zones (Yeo and Flowers, 1984). Acceptance
of the threshold concept in crop-yield response requires acceptance of the thermodynamic premise that plants with such mechanisms develop and operate at a constant growth capacity regardless of the magnitude of the root-zone salt concentration (Soo, 1962). That is, the biological energy utilized to grow and operate salt-tolerance mechanisms up to \( C_t \) is constant and unrelated to crop yield. A continuous, though small and increasing, crop-yield decline at pre-\( C_t \) salinity levels would seem to support more plausible thermodynamic logic.

Relating \( Y_t \) to \( C/C_{50} \) by the modified discount function (Eq. [9]), wherein \( s \), the steepness component, is fixed in values from 0.001 through 0.22 and \( C_{50} = 10 \text{ dS m}^{-1} \), results in an array of response curves with a common point at \( C/C_{50} = 1.0 \) (Fig. 7). The change in \( Y_t \) with a unit change in \( C/C_{50} \) for different values of \( s \) is not linear. Figure 8 shows changes in relative yield as a function of relative salinity for four unit changes in parameter \( s \). The plots in Fig. 8 indicate that a maximum change of 15% in \( Y_t \) is associated with a \( C/C_{50} \) value near 0.35 as \( s \) varies from 0.001 to 0.069. This maximum change in \( Y_t \) decreases with increases in \( s \) and with shifts to higher \( C/C_{50} \) values. If \( s \) is constant, an increasing value of \( C_{50} \) results in relative crop yields \( (Y_t) \) which differ depending on the value of \( C \). Three plots of the differences in \( Y_t \) for three changes in \( C \) plotted with increasing \( C_{50} \) and \( s = 0.11 \) reveal that percentage differences in relative yield do not exceed 11% of a unit difference in root-zone salinity and that percentages decrease as \( C \) increases (Fig. 9).

Acceptance of the continuous, discount response function for crop yield with increasing root-zone salinity also accepts the threshold-slope function as an approximation. This implies that the parameters of the two functions are related and can be derived from relationships based on each other. For example, if \( C_t \) and \( b \) are known for any crop, it should be possible to estimate \( C_{50} \) and \( s \) from them. Various methods for deriving \( C_{50} \) and \( s \) from \( C_t \) and \( b \) are explored, and the best procedures for the conversions are selected in the companion.

Table 2. Parameters and statistical results from regression analyses of six functions relating relative Biggar wheat yields \( (Y_t) \) to root-zone salinity \( (C = EC_t) \).

<table>
<thead>
<tr>
<th>Function</th>
<th>Equation</th>
<th>( R^2 )</th>
<th>RMSE</th>
<th>Parameter values (units omitted)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Simple Linear</td>
<td>( Y_t = a - b(C) )</td>
<td>0.941</td>
<td>0.09398</td>
<td>( a = 1.0350 ) ( b = 0.0811 )</td>
</tr>
<tr>
<td>Weibull</td>
<td>( Y_t = \exp[a(C)^c] )</td>
<td>0.984</td>
<td>0.05058</td>
<td>( a = -0.0289 ) ( b = 1.8226 )</td>
</tr>
<tr>
<td>Bi-Exponential</td>
<td>( Y_t = \exp[aC - b(C)] )</td>
<td>0.982</td>
<td>0.08310</td>
<td>( a = -0.0092 ) ( b = 0.0193 )</td>
</tr>
<tr>
<td>Gompertz</td>
<td>( Y_t = 1 - b(C - C_t) )</td>
<td>0.966</td>
<td>0.07715</td>
<td>( a = -0.0256 ) ( b = 0.03515 )</td>
</tr>
<tr>
<td>Threshold-Slope</td>
<td>( Y_t = \frac{1}{1 + (C/C_{50})^{exp[cb]}} )</td>
<td>0.988</td>
<td>0.04328</td>
<td>( C_{50} = 1.5730 ) ( b = 0.1306 )</td>
</tr>
<tr>
<td>Discount</td>
<td></td>
<td></td>
<td></td>
<td>( C_{50} = 5.442 ) ( s = 0.1838 )</td>
</tr>
</tbody>
</table>
Table 3. Resulting coefficient-of-determination ($R^2$) and root-mean-square-error (RMSE) values derived from threshold-slope and modified-discount response functions for product yields with increasing root-zone salinity in tested agricultural crops.

<table>
<thead>
<tr>
<th>Cultivar</th>
<th>Min–Max</th>
<th>N</th>
<th>$R^2$</th>
<th>RMSE</th>
<th>$R^2$</th>
<th>RMSE</th>
<th>Data source</th>
</tr>
</thead>
<tbody>
<tr>
<td>Alfalfa (Medicago sativa L.; M. falcata L.)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Beaver</td>
<td>0.7–14</td>
<td>8</td>
<td>0.930</td>
<td>0.1187</td>
<td>0.972</td>
<td>0.0746</td>
<td>Steppuhn et al., 1999</td>
</tr>
<tr>
<td>Rangelander</td>
<td>0.7–14</td>
<td>8</td>
<td>0.866</td>
<td>0.1629</td>
<td>0.997</td>
<td>0.0233</td>
<td>Steppuhn et al., 1999</td>
</tr>
<tr>
<td>Calif. common</td>
<td>2–18</td>
<td>4</td>
<td>0.957</td>
<td>0.0626</td>
<td>0.964</td>
<td>0.0577</td>
<td>Brown and Hayward, 1956</td>
</tr>
<tr>
<td>Barley (Hordeum vulgare L.)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Bonanza</td>
<td>0.75–19</td>
<td>15</td>
<td>0.867</td>
<td>0.1136</td>
<td>0.972</td>
<td>0.0522</td>
<td>STTL, 1990</td>
</tr>
<tr>
<td>Bonanza</td>
<td>0.75–18</td>
<td>12</td>
<td>0.924</td>
<td>0.1053</td>
<td>0.968</td>
<td>0.0685</td>
<td>Steppuhn, 1993</td>
</tr>
<tr>
<td>Bridge</td>
<td>0.75–19</td>
<td>15</td>
<td>0.944</td>
<td>0.0758</td>
<td>0.975</td>
<td>0.0504</td>
<td>STTL, 1990</td>
</tr>
<tr>
<td>Bridge</td>
<td>0.75–18</td>
<td>12</td>
<td>0.935</td>
<td>0.0988</td>
<td>0.938</td>
<td>0.0968</td>
<td>Steppuhn, 1993</td>
</tr>
<tr>
<td>Harrington</td>
<td>0.75–19</td>
<td>15</td>
<td>0.832</td>
<td>0.0996</td>
<td>0.951</td>
<td>0.0538</td>
<td>STTL, 1990</td>
</tr>
<tr>
<td>Harrington</td>
<td>0.5–16</td>
<td>7</td>
<td>0.944</td>
<td>0.0992</td>
<td>0.976</td>
<td>0.0650</td>
<td>Steppuhn et al., 2004</td>
</tr>
<tr>
<td>Canola (Brassica napus L.)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Hyola 401‡</td>
<td>0.5–16</td>
<td>7</td>
<td>0.911</td>
<td>0.1418</td>
<td>0.955</td>
<td>0.1010</td>
<td>STTL, 1990</td>
</tr>
<tr>
<td>Hyola 401§</td>
<td>0.75–14</td>
<td>7</td>
<td>0.946</td>
<td>0.0950</td>
<td>0.950</td>
<td>0.0921</td>
<td>Steppuhn et al., 2004</td>
</tr>
<tr>
<td>InVigor2573§</td>
<td>0.75–14</td>
<td>7</td>
<td>0.894</td>
<td>0.1462</td>
<td>0.988</td>
<td>0.0497</td>
<td>Steppuhn et al., 2004</td>
</tr>
<tr>
<td>Quantum‡</td>
<td>0.5–16</td>
<td>7</td>
<td>0.946</td>
<td>0.1023</td>
<td>0.938</td>
<td>0.1096</td>
<td>Steppuhn et al., 2004</td>
</tr>
<tr>
<td>Carrot (Daucus carota L.)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Early French</td>
<td>0.625–7.5</td>
<td>12</td>
<td>0.795</td>
<td>0.1563</td>
<td>0.978</td>
<td>0.0546</td>
<td>Magistad et al., 1943; Osawa, 1965</td>
</tr>
<tr>
<td>Foxtail, meadow (Alopecurus pratensis L.)</td>
<td></td>
<td></td>
<td></td>
<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>unknown</td>
<td>1–14.5</td>
<td>8</td>
<td>0.958</td>
<td>0.0718</td>
<td>0.997</td>
<td>0.188</td>
<td>Brown and Bernstein, 1953</td>
</tr>
<tr>
<td>Harding-grass (Lolium perenne L.)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>Bonel</td>
<td>5.8–15.9</td>
<td>6</td>
<td>0.527</td>
<td>0.1653</td>
<td>0.604</td>
<td>0.1448</td>
<td>Francois et al., 1989</td>
</tr>
<tr>
<td>Sorghum (Sorghum bicolor (L.) Moench)</td>
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<td></td>
<td></td>
<td></td>
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<tr>
<td>NK-265</td>
<td>3–12.4</td>
<td>12</td>
<td>0.742</td>
<td>0.1408</td>
<td>0.774</td>
<td>0.1293</td>
<td>Brown and Bernstein, 1953</td>
</tr>
<tr>
<td>Sugarbeet (Beta vulgaris L.)</td>
<td></td>
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<tr>
<td>unknown</td>
<td>0.95–10.3</td>
<td>7</td>
<td>0.905</td>
<td>0.1202</td>
<td>0.972</td>
<td>0.0670</td>
<td>Francois et al., 1984</td>
</tr>
<tr>
<td>Tomato (Lycopersicon lycopersicum (L.) Karsten)</td>
<td></td>
<td></td>
<td></td>
<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>unknown</td>
<td>1–14</td>
<td>6</td>
<td>0.808</td>
<td>0.1646</td>
<td>0.982</td>
<td>0.0499</td>
<td>Osawa, 1965</td>
</tr>
<tr>
<td>Turnip (Brassica rapa L.)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Purple-top</td>
<td>0.9–8.3</td>
<td>4</td>
<td>0.980</td>
<td>0.0360</td>
<td>0.998</td>
<td>0.0139</td>
<td>Francois, 1984</td>
</tr>
<tr>
<td>Wheat, durum (Triticum turgidum L. var. durum Desf.)</td>
<td>1–9</td>
<td>10</td>
<td>0.781</td>
<td>0.180</td>
<td>0.965</td>
<td>0.040</td>
<td>Steppuhn et al., 1996</td>
</tr>
<tr>
<td>Wheat, spring (Triticum aestivum L.)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Neepawa</td>
<td>1–14</td>
<td>12</td>
<td>0.775</td>
<td>0.100</td>
<td>0.953</td>
<td>0.040</td>
<td>Steppuhn et al., 1996</td>
</tr>
<tr>
<td>Biggar</td>
<td>1–14</td>
<td>12</td>
<td>0.692</td>
<td>0.170</td>
<td>0.934</td>
<td>0.060</td>
<td>Steppuhn et al., 1996</td>
</tr>
<tr>
<td>Katepwa</td>
<td>1–14</td>
<td>10</td>
<td>0.754</td>
<td>0.200</td>
<td>0.890</td>
<td>0.100</td>
<td>Steppuhn et al., 1996</td>
</tr>
<tr>
<td>Fielder</td>
<td>1–14</td>
<td>10</td>
<td>0.717</td>
<td>0.230</td>
<td>0.730</td>
<td>0.260</td>
<td>Steppuhn et al., 1996</td>
</tr>
<tr>
<td>Wheatgrass, green (Elymus hoffmannii Jensen &amp; Asay)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Saltlander§</td>
<td>0.75–25</td>
<td>8</td>
<td>0.824</td>
<td>0.1798</td>
<td>0.961</td>
<td>0.0849</td>
<td>Steppuhn and Asay, 2004</td>
</tr>
<tr>
<td>Saltlander‡</td>
<td>0.75–24</td>
<td>9</td>
<td>0.799</td>
<td>0.1988</td>
<td>0.985</td>
<td>0.0546</td>
<td>Steppuhn and Asay, 2004</td>
</tr>
<tr>
<td>Wheatgrass (Elymus hoffmannii Jensen &amp; Asay)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NewHy</td>
<td>0.75–24</td>
<td>9</td>
<td>0.700</td>
<td>0.1800</td>
<td>0.985</td>
<td>0.0414</td>
<td>Steppuhn and Asay, 2004</td>
</tr>
<tr>
<td>Wheatgrass, tall [= Thinopyron ponticum (Podp.) Liu &amp; Wang]</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Orbi§</td>
<td>0.75–25</td>
<td>8</td>
<td>0.912</td>
<td>0.1163</td>
<td>0.970</td>
<td>0.0677</td>
<td>Steppuhn and Asay, 2004</td>
</tr>
<tr>
<td>Orbi‡</td>
<td>0.75–24</td>
<td>9</td>
<td>0.810</td>
<td>0.1699</td>
<td>0.979</td>
<td>0.0562</td>
<td>Steppuhn and Asay, 2004</td>
</tr>
</tbody>
</table>

† STTL, unpublished data, Canada’s Salinity Tolerance Testing Lab.
‡ Predominately chloride salts.
§ Predominately sulfate salts.

As briefly reviewed in this study, many factors influence the yield of agricultural crops besides exposure to increasing root-zone salinity. Consequently, the single-value, Salinity Tolerance Index would seem more appropriate for comparing agricultural crops than any of the dual parameters of any of the response functions. The index is based on the nonlinear parameters of $C_{50}$ and $s$ (Eq. [11]). The ST-Index identifies a salinity value equal to the 50% reduction in crop yield from that of the nonsaline yield plus a measure of the tendency to maintain some product yield as the crop is subjected to salinity levels less than but approaching $C_{50}$:

$$\text{ST-Index} = C_{50} + s(C_{50})$$  \[13\]
Table 4. Nonlinear discount parameters and the Salinity Tolerance Index (STI) derived from linear threshold-slope parameters by the conversion methods detailed in the companion paper (Steppuhn et al., 2005).

<table>
<thead>
<tr>
<th>Crop</th>
<th>$b^*$</th>
<th>$C_{t^*}$</th>
<th>$C_{s^*}$</th>
<th>$s^*$</th>
<th>STI</th>
</tr>
</thead>
<tbody>
<tr>
<td>Corn</td>
<td>0.120</td>
<td>1.70</td>
<td>5.54</td>
<td>0.183</td>
<td>6.56</td>
</tr>
<tr>
<td>Alfalfa</td>
<td>0.073</td>
<td>2.00</td>
<td>8.49</td>
<td>0.111</td>
<td>9.43</td>
</tr>
<tr>
<td>Radish</td>
<td>0.130</td>
<td>1.20</td>
<td>4.73</td>
<td>0.198</td>
<td>5.67</td>
</tr>
</tbody>
</table>

* $b^*$, Absolute value of the linear regression slope parameter.
* $C_{t^*}$, “Threshold” salinity parameter.
* $C_{s^*}$, Salinity where crop yield equals 50% of the nonsaline yield.
* $s^*$, Absolute value of the nonlinear steepness parameter.

CONCLUSIONS

Relative crop yield has evolved as the primary indicator of agricultural crop tolerance or resistance to root-zone salinity. Experimental data to evaluate the relative tolerance of crops to salinity require yield response functions which account for the high degree of variability associated with testing for crop yields and include responses from factors other than salinity. With an aim to compare various yield functions to suggest a general empirical response and index which most closely reflect the general agricultural crop response to root-zone salinity, this study has led to the following conclusions.

1. A comparative salinity tolerance index (ST-Index), based on the nonlinear (modified-discount) regression parameters of $C_{50}$ (the salinity level associated with a 50% yield of the relative nonsaline, crop production) and $s$ (the absolute steepness of the general relative yield decline with salinity), can serve to rate agricultural crop tolerance to root-zone salinity [ST-Index = $C_{50} + s(C_{50})$].

2. Of the six response functions applied to data from the spring-wheat cultivar Biggar, the modified-discount, sigmoidal-shape response function $[Y_r = \frac{1}{1 + (C/C_{50})^{s(C_{50})}}]$ gave the lowest root mean square error and the highest $R^2$ value.

3. The modified-discount, nonlinear relationship compared to the threshold-slope linear model for product yield-salinity response data in 33 separate trials (17 crops) averaged 11% closer in statistical fit and 45% lower in statistical error.

4. From sensitivity analyses, a maximum change of 15% or less in relative yield resulted from a 100% change in $s$ or $C_{50}$ of the modified discount function.

5. The availability of nonlinear regression software makes it unnecessary to approximate nonlinear sigmoidal response parameters with parameters derived from linear functions.

6. Various procedures for converting the linear parameters of threshold salinity ($C_t$) and slope ($b$) into the nonlinear parameters of the salinity at 50% yield reduction ($C_{50}$) and the central unit decline in relative yield with salinity ($s$) are explored for a large array of agricultural crops in the companion paper (Steppuhn et al., 2005).
ACKNOWLEDGMENTS

With thanks, the authors acknowledge the valuable contributions of Mr. K.G. Wall, Mr. K.W. Deobald, Dr. Y.W. Jame, Dr. S. Yang-Steppuhn, and staff members of the George E. Brown, Jr. Salinity Laboratory and the Semiarid Prairie Agricultural Research Centre to this research.

REFERENCES


